# Gravity Particles and the Strong Force 

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#### Abstract

This paper displays a graphical model for gravitational particles, so as to determine the wavelength of gravity waves. This wavelength is obtained graphically by trigonometry, in order to compute the gravitational acceleration, due to a body, at any point in space measured from the center of the body. The objective is to determine the gravitational acceleration, the wavelength of the gravitational wave, speed of the wave and its specific internal energy. To do the study we used formulas for acceleration and velocity which were obtained from hypothesis and well sustained experiment. Tables of results are shown which compare the results for gravitational acceleration obtained in this model, the results of Newton's equation and the results for $45^{\circ}$ taken from a book of physics [2]. It is concluded that gravitational force is a strong force and gravitational wave speed equals the speed of light at the center of the earth and diminishes with movement away from its center.


## 1. Introduction

I describe a theoretical graphic model of the duality particle wave, of gravitational waves, in order to calculate the gravitational acceleration at any point of space measured from the center of the earth. This model is inspired from the Reynolds apparatus.

Figures are shown of the theoretical gravitational wave particle which allow us, using examples, to determine its wavelength, the speed of the wave, its specific internal energy and its distance from the center of the earth.

Tables 1 and 2 show the gravitational acceleration calculated for a different number of wavelength particles (Figs. 2 and 3 respectively) at the earth's surface. These are compared with Newton's Eq. (3).

This paper will demonstrate that very short wavelength gravitational particles, on the earth's surface, have the same value as at the center of the earth, where the speed of the gravitational particle is the speed of the light. The gravitational acceleration at the center of the earth, its frequency and its energy are also calculated.

It will also show an example where, for a 12 cm diameter disc located on the surface of the earth, the speed, frequency and energy required to change the acceleration vector to the opposite direction from the gravitational acceleration is calculated.

## 2. List of Symbols

Calculations in this paper will be carried to five significant figures, the limit of the universal gravitational constant $G$ [1].
$h_{P} \quad 6.6261 \times 10^{-34} \mathrm{~J}-\mathrm{s}$, Planck constant
$l_{P} \quad 1.6162 \times 10^{-35} \mathrm{~m}$, Planck length
c $2.9979 \times 10^{8} \mathrm{~m} / \mathrm{s}$, speed of light
G $\quad 6.6730 \times 10^{-11} \mathrm{~N}-\mathrm{m}^{2} / \mathrm{kg}^{2}$, gravitational constant
$M_{e} 5.9742 \times 10^{24} \mathrm{~kg}$, earth mass
$R_{e} \quad 6.3781 \times 10^{6} \mathrm{~m}$, earth radius
$R_{E} 2$ (unitless), Reynolds number
$g_{r}$ gravitational acceleration, calculated ( $\mathrm{m} / \mathrm{s}^{2}$ )
$g_{N}$ gravitational acceleration, Newtonian ( $\mathrm{m} / \mathrm{s}^{2}$ )
$h$ distance from the earth's surface to a point in the space (m)
$r_{P}$ radius of the gravitational particle (m)
$\lambda$ wavelength of a gravitational particle at a point in space (m)
$\lambda_{S}$ wavelength of a gravitational particle at earth's surface (m)
$v_{r}$ threshold speed at equilibrium, gravitational particles ( $\mathrm{m} / \mathrm{s}$ )
$v$ specific internal energy, equivalent to kinematic viscosity
( $\mathrm{m}^{2} / \mathrm{s}=\mathrm{J}-\mathrm{s} / \mathrm{kg}$ )
$f$ frequency ( Hz )
$\omega$ frequency ( $\mathrm{rad} / \mathrm{s}$ )
$\theta$ parameter related to the number of particles

## 3. Theoretical Model



Fig. 1. Theoretical model for gravitational particles
The central circle in Fig. 1 represents the earth. Toward the center of the earth flow four gravitational particles, whose diameters are diminishing as demonstrated. Fig. 2 is an illustration of the magnitude of the gravitational particle wavelength $\lambda$ located at distance $h$ above the earth's surface, and the magnitude of the gravitational particle wavelength $\lambda_{S}$ located at the earth's surface.

The wavelength is the diameter of the gravitational particle at a point in space. Fig. 2 shows the radius $r_{P}$ of a gravitational particle ( $\theta=45^{\circ}$ in the figure),

$$
\begin{equation*}
r_{P}=\left(R_{e}+h\right) \cos \theta \tag{a}
\end{equation*}
$$

but the wavelength $\lambda$ is just the diameter of the particle:

$$
\begin{equation*}
\lambda=2 r_{P}=2\left(R_{e}+h\right) \cos \theta \tag{b}
\end{equation*}
$$



Fig. 2. Gravitational particles model at $\theta=45^{\circ}$.
The equation for gravitational acceleration $g_{r}$ in this study:

$$
\begin{equation*}
g_{r}=\frac{12 v_{r}^{2}}{\pi R_{E} \lambda} \tag{1}
\end{equation*}
$$

The threshold speed for equilibrium of gravity particles:

$$
\begin{equation*}
v_{r}=\frac{2 v}{\lambda} . \tag{2}
\end{equation*}
$$

Newton's equation for gravitational acceleration $g_{N}$ :

$$
\begin{equation*}
g_{N}=\frac{G M_{e}}{\left(R_{e}+h\right)^{2}} \tag{3}
\end{equation*}
$$

## 4. Example: At the Earth's Surface, $\boldsymbol{\theta}=\mathbf{4 5}{ }^{\circ}$

The following calculations apply at the earth's surface ( $h=0$, $\left.\lambda=\lambda_{S}\right)$ at $\theta=45^{\circ}$.

Gravitational acceleration $g$, by Eq. (3):

$$
g_{N}=\frac{G M_{e}}{\left(R_{e}+h\right)^{2}}=\frac{\left(6.6730 \times 10^{-11}\right)\left(5.9742 \times 10^{24}\right)}{\left(6.3781 \times 10^{6}+0\right)^{2}}=9.7998 \mathrm{~m} / \mathrm{s}^{2}
$$

Gravitational wavelength $\lambda=\lambda_{S}$, by Eq. (b):
$\lambda_{S}=2\left(R_{e}+h\right) \cos \theta=2\left(6.3781 \times 10^{6}+0\right) \cos 45^{\circ}=9.0200 \times 10^{6} \mathrm{~m}$
Gravitational particle threshold speed $v_{r}$, by Eq. (1):

$$
v_{r}=\sqrt{\frac{\pi R_{E} g_{N} \lambda}{12}}=\sqrt{\frac{\pi(2)(9.7998)\left(9.0200 \times 10^{6}\right)}{12}}=6803.2 \mathrm{~m} / \mathrm{s}
$$

Gravitational particle specific internal energy $v$, by Eq. (2):

$$
v=\frac{1}{2} v_{r} \lambda=\frac{1}{2}(6803.2)\left(9.0200 \times 10^{6}\right)=3.0682 \times 10^{10} \mathrm{~m}^{2} / \mathrm{s}
$$

Assuming $v$, as just calculated, remains constant at any point in space, where the speed of the gravitational particle $v_{r}=c$, we calculate the following.
Gravitational wavelength $\lambda$, by Eq. (2):

$$
\lambda=\frac{2 v}{c}=\frac{2\left(3.0682 \times 10^{10}\right)}{2.9979 \times 10^{8}}=204.69 \mathrm{~m}
$$

Distance from the earth center $R_{e}+h$, by Eq. (b):

$$
R_{e}+h=\frac{\lambda}{2 \cos \theta}=\frac{204.69}{2 \cos 45^{\circ}}=144.74 \mathrm{~m}
$$

Gravitational acceleration $g_{r}$ at this point, by Eq. (1):

$$
g_{r}=\frac{12 c^{2}}{\pi R_{E} \lambda}=\frac{12\left(2.9979 \times 10^{8}\right)^{2}}{\pi(2)(204.69)}=8.3856 \times 10^{14} \mathrm{~m} / \mathrm{s}^{2}
$$

## 5. Example: Above the Earth, $\theta=45^{\circ}$

The following calculations apply at height $h=100,000 \mathrm{~m}$ above the earth surface, at $\theta=45^{\circ}$. Variables $g_{N}, \lambda, v_{r}$ are given by Eq. (3), (b) and (2) respectively.

$$
\begin{gathered}
g_{N}=\frac{G M_{e}}{\left(R_{e}+h\right)^{2}}=\frac{\left(6.673 \times 10^{-11}\right)\left(5.9742 \times 10^{24}\right)}{\left(6.3781 \times 10^{6}+100,000\right)^{2}}=9.4996 \mathrm{~m} / \mathrm{s}^{2} \\
\lambda=2\left(R_{e}+h\right) \cos \theta=2\left(6.3781 \times 10^{6}+100,000\right) \cos 45^{\circ} \\
=9.1614 \times 10^{6} \mathrm{~m}[=9161 \mathrm{~km}] \\
v_{r}=\frac{2 v}{\lambda}=\frac{2\left(3.0682 \times 10^{10}\right)}{9.1614 \times 10^{6}}=6698.1 \mathrm{~m} / \mathrm{s}
\end{gathered}
$$

Now substitute $v_{r}$ and $\lambda$ into Eq. (1):

$$
g_{r}=\frac{12 v_{r}^{2}}{\pi R_{E} \lambda}=\frac{12(6698.1)^{2}}{\pi(2)\left(9.1614 \times 10^{6}\right)}=9.3528 \mathrm{~m} / \mathrm{s}^{2}
$$

Table 1 shows results obtained for gravitational acceleration for different values of $h$ in Fig. 2. Compare the values obtained between $g_{r}$ in Eq. (1), Newton's $g_{N}$ in Eq. (3), and measured $g_{m}$ for $\theta=45^{\circ}$ given in [2].

| $\boldsymbol{c}$ <br> $\boldsymbol{h}$ <br> $\mathbf{( m )}$ | $\boldsymbol{\lambda}$ <br> $\left(\mathbf{1 0}^{\mathbf{6}} \mathbf{m}\right)$ | $v_{r}$ <br> $(\mathbf{m} / \mathbf{s})$ | $g_{r}$ <br> $\left(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\right)$ | $g_{N}$ <br> $\left(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\right)$ | $g_{m}$ <br> $\left(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\right)$ |
| ---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 9.0200 | 6803.2 | 9.7998 | 9.7998 | 9.806 |
| 1000 | 9.0214 | 6802.1 | 9.7952 | 9.7968 | 9.803 |
| 4000 | 9.0257 | 6798.9 | 9.7814 | 9.7875 | 9.794 |
| 8000 | 9.0313 | 6794.7 | 9.7630 | 9.7753 | 9.782 |
| 16000 | 9.0426 | 6786.2 | 9.7264 | 9.7508 | 9.757 |
| 32000 | 9.0653 | 6769.2 | 9.6538 | 9.7022 | 9.71 |
| 100000 | 9.1614 | 6698.1 | 9.3528 | 9.4996 | 9.60 |
| 500000 | 9.7271 | 6308.6 | 7.7842 | 8.4268 | 8.53 |
| 1000000 | 10.434 | 5881.1 | 6.3308 | 7.3234 | 7.41 |
| $0.38 \mathrm{e}^{9}$ | 546.42 | 112.30 | $4.41 \mathrm{e}^{-5}$ | $2.60 \mathrm{e}^{-3}$ | $2.71 \mathrm{e}^{-3}$ |
| $149 \mathrm{e}^{9}$ | 210730 | 0.2912 | $7.69 \mathrm{e}^{-13}$ | $1.80 \mathrm{e}^{-8}$ | ---- |

Table 1. Calculated properties for $\theta=45^{\circ}$, Fig. 2.

## 6. Example: At the Earth's Surface, $\theta=30^{\circ}$

Fig. 3 shows a model for three gravitational particles flowing to the center of the earth, at the earth surface $\left(h=0, \lambda=\lambda_{S}\right)$ for the case $\theta=30^{\circ}$. Calculate $\lambda=\lambda_{S}, v_{r}, v$ by Eqs. (b), (1) and (2).

$$
\begin{gathered}
\lambda_{S}=2\left(R_{e}+h\right) \cos \theta=2\left(6.3781 \times 10^{6}+0\right) \cos 30^{\circ}=1.1047 \times 10^{7} \mathrm{~m} \\
v_{r}=\sqrt{\frac{\pi R_{E} g \lambda}{12}}=\sqrt{\frac{\pi(2)(9.7998)\left(11.047 \times 10^{6}\right)}{12}}=7528.9 \mathrm{~m} / \mathrm{s} \\
v=\frac{1}{2} v_{r} \lambda=\frac{1}{2}(7528.9)\left(1.1047 \times 10^{7}\right)=4.1586 \times 10^{10} \mathrm{~m}^{2} / \mathrm{s}
\end{gathered}
$$



Fig. 3. Gravitational particles model at $\theta=30^{\circ}$.
Again assuming $v$, as just calculated, remains constant at any point in space, where the speed of the gravitational particle $v_{r}=c$, calculate $\lambda, R_{e}+h$, and $g_{r}$ by (2), (b) and (1).

$$
\begin{gathered}
\lambda=\frac{2 v}{c}=\frac{2\left(4.1586 \times 10^{10}\right)}{2.9979 \times 10^{8}}=277.43 \mathrm{~m} \\
R_{e}+h=\frac{\lambda}{2 \cos \theta}=\frac{277.43}{2 \cos 30^{\circ}}=160.17 \mathrm{~m} \\
g_{r}=\frac{12 c^{2}}{\pi R_{E} \lambda}=\frac{12\left(2.9979 \times 10^{8}\right)^{2}}{\pi(2)(277.43)}=6.1870 \times 10^{14} \mathrm{~m} / \mathrm{s}^{2}
\end{gathered}
$$

## 7. Example: Above the Earth, $\boldsymbol{\theta}=30^{\circ}$

The following calculations apply at height $h=100,000 \mathrm{~m}$ above the earth surface, at $\theta=30^{\circ}$. Variables $\lambda, v_{r}, g_{r}$ are given by Eqs. (b), (2) and (1) respectively.

$$
\begin{gathered}
\lambda=2\left(R_{e}+h\right) \cos \theta=2\left(6.3781 \times 10^{6}+100,000\right) \cos 30^{\circ}=1.1220 \times 10^{6} \mathrm{~m} \\
v_{r}=\frac{2 v}{\lambda}=\frac{2\left(4.1586 \times 10^{10}\right)}{1.1220 \times 10^{6}}=7412.8 \mathrm{~m} / \mathrm{s} \\
g_{r}=\frac{12 v_{r}^{2}}{\pi R_{E} \lambda}=\frac{12(7412.8)^{2}}{\pi(2)\left(1.1220 \times 10^{7}\right)}=9.3530 \mathrm{~m} / \mathrm{s}^{2}
\end{gathered}
$$

Table 2 shows the results obtained for gravitational acceleration for different values of $h$.

| $\boldsymbol{h}$ <br> $\mathbf{( m )})$ | $\boldsymbol{\lambda}$ <br> $\left(\mathbf{( \mathbf { 1 0 } ^ { 7 } \mathbf { m } )}\right.$ | $v_{r}$ <br> $(\mathbf{m} / \mathbf{s})$ | $g_{r}$ <br> $\left(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\right)$ | $g_{\boldsymbol{N}}$ <br> $\left(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\right)$ |
| ---: | :---: | :---: | :---: | :---: |
| 0 | 1.1033 | 7528.9 | 9.7998 | 9.7998 |
| 1000 | 1.1034 | 7527.8 | 9.7952 | 9.7968 |
| 4000 | 1.1040 | 7524.2 | 9.7814 | 9.7875 |
| 8000 | 1.1047 | 7519.5 | 9.7630 | 9.7753 |
| 16000 | 1.1061 | 7510.1 | 9.7264 | 9.7508 |
| 32000 | 1.1088 | 7491.4 | 9.6538 | 9.7022 |
| 100000 | 1.1206 | 7412.8 | 9.3530 | 9.4996 |
| 500000 | 1.1899 | 6981.6 | 7.8142 | 8.4268 |
| 1000000 | 1.2033 | 6508.5 | 6.3308 | 7.3234 |
| $0.38 \mathrm{e}^{9}$ | 66.921 | 124.28 | $4.41 \mathrm{e}^{-5}$ | $2.67 \mathrm{e}^{-3}$ |
| $149 \mathrm{e}^{9}$ | 25808 | 0.3223 | $7.69 \mathrm{e}^{-13}$ | $1.80 \mathrm{e}^{-8}$ |

Table 2. Calculated properties for $\theta=30^{\circ}$, Fig. 3.

## 8. Near the Earth Center

Calculate the distance to the earth center $R_{e}+h$ where the gravitational particle speed is the speed of light, and the wavelength on the earth's surface is $\lambda_{S}=2.2235 \mathrm{~mm}$. On the earth's surface, from Eq. (1):

$$
v_{r}=\sqrt{\frac{\pi R_{E} g \lambda_{S}}{12}}=\sqrt{\frac{\pi(2)(9.7998)\left(2.2235 \times 10^{-3}\right)}{12}}=0.10681 \mathrm{~m} / \mathrm{s}
$$

From Eq. (2):

$$
v=\frac{1}{2} v_{r} \lambda_{S}=\frac{1}{2}(0.10681)\left(2.2235 \times 10^{-3}\right)=1.1874 \times 10^{-4} \mathrm{~m}^{2} / \mathrm{s}
$$

Near the center of the earth, with $v_{r}=c$, from Eq. (2):

$$
\lambda=\frac{2 v}{c}=\frac{2\left(1.1874 \times 10^{-4}\right)}{2.9979 \times 10^{8}}=7.9215 \times 10^{-13} \mathrm{~m}
$$

At this same point near the earth center, by Eq. (b):

$$
R_{e}+h=\frac{\lambda}{2 \cos \theta}=\frac{7.9215 \times 10^{-13}}{2 \cos 89.99999999^{\circ}}=2.2693 \times 10^{-3} \mathrm{~m}=2.2693 \mathrm{~mm}
$$

This value is almost equal to the wavelength on the surface $\lambda_{S}$. The gravitational acceleration $g_{r}$ at this point, from Eq. (1):

$$
g_{r}=\frac{12 c^{2}}{\pi R_{E} \lambda}=\frac{12\left(2.9979 \times 10^{8}\right)^{2}}{\pi(2)\left(7.9215 \times 10^{-13}\right)}=2.1668 \times 10^{29} \mathrm{~m} / \mathrm{s}^{2}
$$

Since $\lambda_{S} \approx R_{e}+h$ for $v_{r}=c$ in the center of the earth, substitute $\lambda_{S}=l_{P}$, the Planck length. Then the gravitational acceleration $g_{P}$ in the center of the earth is:

$$
g_{P}=\frac{12 c^{2}}{\pi R_{E} l_{p}}=\frac{12\left(2.9979 \times 10^{8}\right)^{2}}{\pi(2)\left(1.6162 \times 10^{-35}\right)}=1.0620 \times 10^{52} \mathrm{~m} / \mathrm{s}^{2}
$$

The frequency $\omega$ is:

$$
\omega=\frac{v_{r}}{\lambda}=\frac{c}{l_{p}}=\frac{2.9979 \times 10^{8}}{1.6162 \times 10^{-35}}=1.8549 \times 10^{43} \mathrm{rad} / \mathrm{s}
$$

or

$$
f=\frac{\omega}{2 \pi}=2.96562 \times 10^{42} \mathrm{~Hz}
$$

The energy is:

$$
E=h_{P} f=\left(6.6261 \times 10^{-34}\right)\left(1.8549 \times 10^{43}\right)=1.2291 \times 10^{10} \mathrm{~J}
$$

| Fig. | Particles | $R_{e}+h$ <br> $(\mathbf{m})$ | $g_{r}$ <br> $\left(\mathbf{m} / \mathbf{s}^{2}\right)$ | $\theta$ <br> $($ degrees $)$ |
| :---: | :---: | :---: | :---: | :---: |
| 3 | 3 | 160.17 | $6.1870 \mathrm{e}^{14}$ | $30^{\circ}$ |
| 2 | 4 | 144.74 | $8.3856 \mathrm{e}^{14}$ | $45^{\circ}$ |
| 4 | $1.8 \mathrm{e}^{10}$ | $2.2693 \mathrm{e}^{-3}$ | $2.1668 \mathrm{e}^{29}$ | $89.99999999^{\circ}$ |

Table 3. Calculated accelerations for $R_{e}+h, v_{r}=c$, at various $\theta$
Table 3 shows that the higher the number of particles around the earth, the shorter the distance from the center of the earth, where $v_{r}=c$ and the strength of the gravity is highest. $R_{e}+h$ is the distance to the Earth's center, and "Particles" means the number of particles around the Earth.


Fig. 4. Schematized for the shortest wavelength $\lambda_{S}=2.2235 \mathrm{~mm}$.

## 9. Gravity Wave through a Disk

Calculate of the threshold speed for equilibrium $v_{r}$, internal specific energy $v$, for the gravitational wave flowing through a disc of diameter $\lambda=12 \mathrm{~cm}=0.12 \mathrm{~m}$ located on the earth's surface. From Eq. (1):

$$
v_{r}=\sqrt{\frac{\pi R_{E} g \lambda}{12}}=\sqrt{\frac{\pi(2)(9.7998)(0.12)}{12}}=0.78469 \mathrm{~m} / \mathrm{s}
$$

From Eq. (2):

$$
v=\frac{1}{2} v_{r} \lambda_{S}=\frac{1}{2}(0.78469)(0.12)=0.047081 \mathrm{~m}^{2} / \mathrm{s}
$$

The frequency $\omega$ is:
or

$$
\omega=\frac{v_{r}}{\lambda}=\frac{2 v}{\lambda^{2}}=\frac{2(0.047081)}{(0.12)^{2}}=6.5390 \mathrm{rad} / \mathrm{s}
$$

$$
f=\frac{\omega}{2 \pi}=1.0407 \mathrm{~Hz}
$$

And the energy is:

$$
E=h_{P} f=\left(6.6261 \times 10^{-34}\right)(6.5390)=4.3328 \times 10^{-33} \mathrm{~J}
$$

## 10. Conclusion

The speed of the gravity wave is equal to the speed of light at a point located at a distance equal to the Planck length from the earth's center. This speed variation is from $c=3 \times 10^{8} \mathrm{~m} / \mathrm{s}$ at this point to zero in the infinite.

The gravity waves can have any value of wavelength. The wavelength of the gravity wave is directly proportional to its specific internal energy and its speed. The gravitational acceleration at a point located at the Planck length from the earth center is $g_{P}=1.0620 \times 10^{52} \mathrm{~m} / \mathrm{s}^{2}$, which makes the gravitational energy $E=4.3328 \times 10^{-33} \mathrm{~J}$. This behaves like the strong force, because next to the earth's center any unit of mass experiences a strong gravity acceleration.

Gravity calculated for the distance earth-moon using Eq. (1) and Newton Eq. (3) has a ratio of 6 which is the same ratio between earth and moon.

We invite experiments which build a coil capable of generating electromagnetic waves at different speeds which coincide with the speed of the gravitational wave for a specific wavelength (the diameter of the coil) and distance from the earth's surface. Maybe it will let us obtain levitation and displacement.

Like an explanatory, all the calculations were made using five significant figures in order to do not clutter the tables 1 and 2 , but it is necessary consider the higher quantity of digits in order to obtain precise expected measurements about speed and wavelength in experiments like LIGO project. In the other hand, Eqs. (1) and (2) were obtained linearly, and perhaps corrections will be needed.

## Appendix [2]

Art. 16-6 Vartaciones de la acelerbacion debidas a la... 525 TABLA 16-1. VARIACIONES DE $g$ CON LA ALTITUD A LA LATITUD DE $45^{\circ}$

| Altitud, <br> metros | $g$, <br> $\mathrm{m} / \mathrm{seg}^{2}$ | Altitud, <br> metros | $\boldsymbol{g}$, <br> $\mathrm{m} / \mathrm{seg}^{2}$ |
| ---: | ---: | ---: | :--- |
| 0 | 9.806 | 32000 | 9.71 |
| 1000 | 9.803 | 100000 | 9.60 |
| 4000 | 9.794 | 500000 | 8.53 |
| 8000 | 9.782 | $1000000^{1}$ | 7.41 |
| 16000 | 9.757 | $380000000^{2}$ | 0.00271 |

${ }^{1}$ Altura de un satélite típico ( $=1000 \mathrm{~km}$ ).
${ }^{2}$ Radio de la órbita de la Luna ( $=386000 \mathrm{~km}$ ).
una esfera. Obtuvo un valor de 7400 km , en comparación con el valor moderno de 6371 km . Esta información fundamental relativa a la forma de la Tierra se fue olvidando gradualmente y no se redescubrió sino hasta la época de los grandes viajes de exploración del siglo xv.

Posteriormente, las mediciones indicaron que, como una buena segunda aproximación, el geoide no es una esfera sino un elipsoide de revolución, achatado a lo largo del eje de rotación de la Tierra y ensanchado en el ecuador. De hecho, el radio ecuatorial excede en 21 km al radio polar. Este achatamiento es motivado por los efectos centrífugos en la Tierra plástica en rotación. La superficie del geoide no es exactamente elipsoidal, se encuentra fuera del elipsoide que más se le ajusta, bajo las masas de montañas, y dentro de él, en los océanos.

El hecho de que el ecuador se encuentra más lejos del centro de la Tierra que lo que están los polos significa que debe haber un aumento constante en el valor medio de $g$ al avanzar del ecuador (latitud $0^{\circ}$ ) a cualquier polo (latitud $90^{\circ}$ ). Esto es lo que se ve en la Tabla 16-2. Sin embargo, como lo muestra el Ej. 2, aproximadamente la mitad de esta variación se puede explicar por otro efecto, a saber, el cambio en el valor efectivo de $g$ producido por la rotación de la Tierra. Por ejemplo, si la Tierra estuviera girando con suficiente rapidez, los objetos colocados en su superficie en el ecuador parecerian

TABLA 16-2. VARIACION DE $g$ CON LA LATITUD AL NIVEL DEL MAR

| Latitud | $g$, <br> $\mathrm{m} / \mathrm{seg}^{2}$ | Latitud | $g$, <br> $\mathrm{m} / \mathrm{seg}^{2}$ |
| :---: | :---: | :---: | :---: |
| $0^{\circ}$ | 9.78039 | $50^{\circ}$ | 9.81071 |
| $10^{\circ}$ | 9.78195 | $60^{\circ}$ | 9.81918 |
| $20^{\circ}$ | 9.78641 | $70^{\circ}$ | 9.82608 |
| $30^{\circ}$ | 9.79329 | $80^{\circ}$ | 9.83059 |
| $40^{\circ}$ | 9.80171 | $90^{\circ}$ | 9.88217 |

## References

[1] http://physics.nist.gov/cuu/Constants/index.html.
[2] Robert Resnick \& David Halliday, Fisica, Parte I, p. 525 (CIA. Editorial Continental, 1977).

